

Package: mfaces (via r-universe)

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Title Fast Covariance Estimation for Multivariate Sparse Functional Data

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Description Multivariate functional principal component analysis via fast covariance estimation for multivariate sparse functional data or longitudinal data proposed by Li, Xiao, and Luo (2020) <doi:10.1002/sta4.245>.

Depends R (>= 2.1.4)

Imports stats, splines, Matrix, matrixcalc, mgcv, face

License GPL-3

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mfaces-package *mfaces*

Description

Fast Covariance Estimation for Multivariate Sparse Functional Data

Details

Package: mfaces
Type: Package
Version: 0.1-4
Date: 2022-07-18
License: GPL-3

Author(s)

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References

Cai Li, Luo Xiao, and Sheng Luo, 2020. Fast covariance estimation for multivariate sparse functional data. *Stat*, 9(1), p.e245, doi:[10.1002/sta4.245](https://doi.org/10.1002/sta4.245).

mface.sparse *Fast covariance estimation for multivariate sparse functional data*

Description

The function is to estimate the mean and covariance function from a cluster of multivariate functions/longitudinal observations.

Usage

```
mface.sparse(data, newdata = NULL,  
             center = TRUE, argvals.new = NULL, knots = 7,  
             knots.option = "equally-spaced",  
             p = 3, m = 2,  
             lambda = NULL, lambda.mean = NULL, lambda.bps = NULL,  
             search.length = 14, lower = -3, upper = 10,  
             calculate.scores = FALSE, pve = 0.99)
```

Arguments

<code>data</code>	a list containing all functional outcomes. Each element is a data frame with three arguments: (1) <code>argvals</code> : observation times; (2) <code>subj</code> : subject indices; (3) <code>y</code> : values of observations for each dimension. Missing values not allowed.
<code>newdata</code>	of the same structure as <code>data</code> ; defaults to <code>NULL</code> , then no prediction.
<code>center</code>	logical. If <code>TRUE</code> , then P-spline smoothing of the population mean will be conducted and subtracted from the data before covariance smoothing; if <code>FALSE</code> , then the population mean will be just 0s.
<code>argvals.new</code>	a vector of observation time points to evaluate mean function, covariance function, error variance and etc. If <code>NULL</code> , then 100 equidistant points in the range of data time points will be used.
<code>knots</code>	the number of knots for B-spline basis functions to be used; defaults to 7. The resulting number of basis functions is the number of interior knots plus the degree of B-splines.
<code>knots.option</code>	if <code>knots</code> specifies the number of knots, then <code>knots.option</code> will be used. Default "equally-spaced", then equally-spaced knots in the range of observed time points will be selected; alternatively, "quantile": quantiles of the observed time points will be selected; see details.
<code>p</code>	the degrees of B-splines; defaults to 3.
<code>m</code>	the order of differencing penalty; defaults to 2.
<code>lambda</code>	the value of the smoothing parameter for auto-covariance smoothing; defaults to <code>NULL</code> .
<code>lambda_mean</code>	the value of the smoothing parameter for mean smoothing; defaults to <code>NULL</code> .
<code>lambda_bps</code>	the value of the smoothing parameter for cross-covariance smoothing; defaults to <code>NULL</code> .
<code>search.length</code>	the number of equidistant (log scale) smoothing parameters to search; defaults to 14.
<code>lower, upper</code>	bounds for log smoothing parameter; defaults are -3 and 10, respectively.
<code>calculate.scores</code>	if <code>TRUE</code> , scores will be calculated.
<code>pve</code>	Defaults 0.99. To select the number of eigenvalues by percentage of variance.

Details

This is a generalized version of bivariate P-splines (Eilers and Marx, 2003) for covariance smoothing of multivariate sparse functional or longitudinal data. It uses tensor product B-spline basis functions and employs differencing penalties on the associated parameter matrix. The smoothing parameters in the method are selected by leave-one-subject-out cross validation and is implemented with a fast algorithm.

If `center` is `TRUE`, then the population means will be calculated and are smoothed by univariate P-spline smoothing: `pspline` (Eilers and Marx, 1996). This univariate smoothing uses leave-one-subject-out cross validation to select the smoothing parameter.

If `knots.option` is "equally-spaced", then the differencing penalty in Eilers and Marx (2003) is used; if `knots.option` is "quantile" then the integrated squared second order derivative penalty in Wood (2016) is used.

Value

`fit` Univariate FPCA fit for each function
`y.pred`, `mu.pred`, `Chat.diag.pred`, `se.pred`, `var.error.pred`
 Predicted/estimated objects at `newdata$argvals`
`Theta` Estimated parameter matrix
`argvals.new` Vector of time points to evaluate population parameters
`Chat.new`, `Cor.new`, `Cor.raw.new`, `Chat.raw.diag.new`, `var.error.new`
 Estimated objects at `argvals.new`
`eigenfunctions`, `eigenvalues`
 Estimated eigenfunctions (scaled eigenvector) and eigenvalues at `argvals.new`
`var.error.hat` Estimated objects for each outcome
`calculate.scores`, `rand_eff`
 if `calculate.scores` is TRUE (default to FALSE), then predicted scores `rand_eff$scores`
 will be calculated.
`...` ...

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References

Cai Li, Luo Xiao, and Sheng Luo, 2020. Fast covariance estimation for multivariate sparse functional data. *Stat*, 9(1), p.e245, doi:[10.1002/sta4.245](https://doi.org/10.1002/sta4.245).
 Luo Xiao, Cai Li, William Checkley and Ciprian Crainiceanu, Fast covariance estimation for sparse functional data, *Stat. Comput.*, doi:[10.1007/s1122201797448](https://doi.org/10.1007/s1122201797448).
 Paul Eilers and Brian Marx, Multivariate calibration with temperature interaction using two-dimensional penalized signal regression, *Chemometrics and Intelligent Laboratory Systems* 66 (2003), 159-174.
 Paul Eilers and Brian Marx, Flexible smoothing with B-splines and penalties, *Statist. Sci.*, 11, 89-121, 1996.
 Simon N. Wood, P-splines with derivative based penalties and tensor product smoothing of unevenly distributed data, *Stat. Comput.*, doi:[10.1007/s112220169666x](https://doi.org/10.1007/s112220169666x).

See Also

`face.sparse` in `face`

Examples

```
## a toy example
## settings
n <- 25
sigma <- 0.1
seed <- 118

set.seed(seed)
```

```

## data generation
N1 <- sample(3:7,n,replace=TRUE)
N2 <- sample(3:7,n,replace=TRUE)
N3 <- sample(3:7,n,replace=TRUE)

subj1 <- c()
subj2 <- c()
subj3 <- c()
for(i in 1:n){
  subj1 <- c(subj1,rep(i, N1[i]))
  subj2 <- c(subj2,rep(i, N2[i]))
  subj3 <- c(subj3,rep(i, N3[i]))
}
t1 <- runif(sum(N1))
t2 <- runif(sum(N2))
t3 <- runif(sum(N3))
tnew <- seq(0,1,length=100)
y1 <- 5*sin(2*pi*t1)
y2 <- 5*cos(2*pi*t2)
y3 <- 5*(t3-1)^2

x1 <- t(matrix(rep(5*sin(2*pi*tnew),n),length(tnew),n))
x2 <- t(matrix(rep(5*cos(2*pi*tnew),n),length(tnew),n))
x3 <- t(matrix(rep(5*(tnew-1)^2,n),length(tnew),n))

psi11 <- function(x){sqrt(2/3)*sin(2*pi*x)}
psi12 <- function(x){sqrt(2/3)*cos(4*pi*x)}
psi13 <- function(x){sqrt(2/3)*sin(4*pi*x)}

psi21 <- function(x){sqrt(2/3)*sin((1-1/2)*pi*x)}
psi22 <- function(x){sqrt(2/3)*sin((2-1/2)*pi*x)}
psi23 <- function(x){sqrt(2/3)*sin((3-1/2)*pi*x)}

psi31 <- function(x){sqrt(2/3)*sin(1*pi*x)}
psi32 <- function(x){sqrt(2/3)*sin(2*pi*x)}
psi33 <- function(x){sqrt(2/3)*sin(3*pi*x)}

Lambda <- c(2,1,0.5)*3

x <- matrix(NA,nrow=n*length(tnew),ncol=3)
xi <- matrix(NA,nrow=n,ncol=3)
for(k in 1:3){xi[,k] = rnorm(n)*sqrt(Lambda[k])}

for(i in 1:n){
  seq1 <- (sum(N1[1:i])-N1[i]+1):(sum(N1[1:i]))
  seq2 <- (sum(N2[1:i])-N2[i]+1):(sum(N2[1:i]))
  seq3 <- (sum(N3[1:i])-N3[i]+1):(sum(N3[1:i]))

  Xt = xi[i,1]*c(psi11(t1[seq1]),psi21(t2[seq2]),psi31(t3[seq3])) +
    xi[i,2]*c(psi12(t1[seq1]),psi22(t2[seq2]),psi32(t3[seq3])) +
    xi[i,3]*c(psi13(t1[seq1]),psi23(t2[seq2]),psi33(t3[seq3]))
}

```

```

y1[seq1] = y1[seq1] + Xt[1:N1[i]]
y2[seq2] = y2[seq2] + Xt[N1[i]+1:N2[i]]
y3[seq3] = y3[seq3] + Xt[N1[i]+N2[i]+1:N3[i]]

x[((i-1)*length(tnew)+1):(length(tnew)*i),] = c(x1[i,], x2[i,], x3[i,]) +
  xi[i,1]*c(psi11(tnew),psi21(tnew),psi31(tnew)) +
  xi[i,2]*c(psi12(tnew),psi22(tnew),psi32(tnew)) +
  xi[i,3]*c(psi13(tnew),psi23(tnew),psi33(tnew))
}

True_C <- Lambda[1]*c(psi11(tnew),psi21(tnew),psi31(tnew))%%
  t(c(psi11(tnew), psi21(tnew), psi31(tnew))) +
  Lambda[2]*c(psi12(tnew), psi22(tnew), psi32(tnew))%%
  t(c(psi12(tnew), psi22(tnew), psi32(tnew))) +
  Lambda[3]*c(psi13(tnew), psi23(tnew), psi33(tnew))%%
  t(c(psi13(tnew), psi23(tnew), psi33(tnew)))

## observed data
y1 <- y1 + rnorm(sum(N1))*sigma
y2 <- y2 + rnorm(sum(N2))*sigma
y3 <- y3 + rnorm(sum(N3))*sigma

# true trajectories
x1 <- t(matrix(x[,1],length(tnew),n))
x2 <- t(matrix(x[,2],length(tnew),n))
x3 <- t(matrix(x[,3],length(tnew),n))

true_eigenfunctions <- eigen(True_C)$vectors*sqrt(length(tnew))
true_eigenvalues <- eigen(True_C)$values/length(tnew)

## organize data and apply mFACES
data <- list("y1" = data.frame("subj"= subj1, "args" = t1, "y" = y1),
  "y2" = data.frame("subj"= subj2, "args" = t2, "y" = y2),
  "y3" = data.frame("subj"= subj3, "args" = t3, "y" = y3))
fit <- mface.sparse(data, args.new = tnew, knots = 5)

## set calculate.scores to TRUE if want to get scores
fit <- mface.sparse(data, args.new = tnew, knots = 5, calculate.scores = TRUE)
scores <- fit$rand_eff$scores

## prediction of several subjects
for(i in 1:2){
  sel <- lapply(data, function(x){which(x$subj==i)})
  dat_i <- mapply(function(data, sel){data[sel,]},
    data = data, sel = sel, SIMPLIFY = FALSE)
  dat_i_pred <- lapply(dat_i, function(x){
    data.frame(subj=rep(x$subj[1],nrow(x) + length(tnew)),
      args = c(rep(NA,nrow(x)),tnew),
      y = rep(NA,nrow(x) + length(tnew)))
  })
}

```

```

})
for(j in 1:length(dat_i)){
  dat_i_pred[[j]][1:nrow(dat_i[[j])], ] <- dat_i[[j]]
}
pred <- predict(fit, dat_i_pred)
y_pred <- mapply(function(pred_y.pred, dat_i){
  pred_y.pred[nrow(dat_i)+1:length(tnew)]}, pred_y.pred = pred$y.pred,
  dat_i = dat_i, SIMPLIFY = TRUE)

pre <- pred

Ylim = c(-12,12)
Xlim = c(0,1)
Ylab = bquote(y^(1))
Xlab = "t"
main = paste("Subject ", dat_i[[1]][1,1],sep="")
idx = (nrow(dat_i[[1]])+1):(nrow(dat_i[[1]])+length(tnew))
plot(dat_i[[1]][, "argvals"], dat_i[[1]][, "y"], ylim=Ylim, xlim=Xlim, ylab=Ylab, xlab=Xlab,
  main=main, cex.lab=2.0, cex.axis = 2.0, cex.main = 2.0, pch=1)
lines(tnew, pre$y.pred$y1[idx], col="red", lwd=2)
lines(tnew, pre$y.pred$y1[idx]-1.96*pre$se.pred$y1[idx], col="blue", lwd=2, lty=2)
lines(tnew, pre$y.pred$y1[idx]+1.96*pre$se.pred$y1[idx], col="blue", lwd=2, lty=2)
lines(tnew, x1[i,], col="purple", lwd=2)

Ylab = bquote(y^(2))
Xlab = "t"
main = paste("Subject ", dat_i[[1]][1,1],sep="")
idx = (nrow(dat_i[[2]])+1):(nrow(dat_i[[2]])+length(tnew))
plot(dat_i[[2]][, "argvals"], dat_i[[2]][, "y"], ylim=Ylim, xlim=Xlim, ylab=Ylab, xlab=Xlab,
  main=main, cex.lab=2.0, cex.axis = 2.0, cex.main = 2.0, pch=1)
lines(tnew, pre$y.pred$y2[idx], col="red", lwd=2)
lines(tnew, pre$y.pred$y2[idx]-1.96*pre$se.pred$y2[idx], col="blue", lwd=2, lty=2)
lines(tnew, pre$y.pred$y2[idx]+1.96*pre$se.pred$y2[idx], col="blue", lwd=2, lty=2)
lines(tnew, x2[i,], col="purple", lwd=2)

Ylab = bquote(y^(3))
Xlab = "t"
main = paste("Subject ", dat_i[[1]][1,1],sep="")
idx = (nrow(dat_i[[3]])+1):(nrow(dat_i[[3]])+length(tnew))
plot(dat_i[[3]][, "argvals"], dat_i[[3]][, "y"], ylim=Ylim, xlim=Xlim, ylab=Ylab, xlab=Xlab,
  main=main, cex.lab=2.0, cex.axis = 2.0, cex.main = 2.0, pch=1)
lines(tnew, pre$y.pred$y3[idx], col="red", lwd=2)
lines(tnew, pre$y.pred$y3[idx]-1.96*pre$se.pred$y3[idx], col="blue", lwd=2, lty=2)
lines(tnew, pre$y.pred$y3[idx]+1.96*pre$se.pred$y3[idx], col="blue", lwd=2, lty=2)
lines(tnew, x3[i,], col="purple", lwd=2)

}

```

Description

Internal function.

Value

No return value, called for internal usage

predict.mface.sparse *Subject-specific curve prediction from a mface.sparse fit*

Description

Predict subject-specific curves based on a fit from "mface.sparse".

Usage

```
## S3 method for class 'mface.sparse'
predict(object, newdata, calculate.scores = T, ...)
```

Arguments

object	a fitted object from the R function "mface.sparse".
newdata	a list containing all functional outcomes. Each element is a data frame with three arguments: (1) argvals: observation times; (2) subj: subject indices; (3) y: values of observations for each dimension. NA values are allowed in "y" but not in the other two.
calculate.scores	if TRUE, scores will be calculated.
...	further arguments passed to or from other methods.

Details

This function makes prediction based on observed data for each subject. So for each subject, it requires at least one observed data. For the time points prediction is desired but no observation is available, just make the corresponding data\$y as NA.

Value

object	A "mface.sparse" fit
newdata	Input data
y.pred, mu.pred, se.pred, Chat.diag.pred, var.error.pred	Predicted/estimated objects at the observation time points in newdata
rand_eff	if calculate.scores in object is TRUE (typically TRUE), then predicted scores rand_eff\$scores will be calculated.
...	...

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References

Cai Li, Luo Xiao, and Sheng Luo, 2020. Fast covariance estimation for multivariate sparse functional data. *Stat*, 9(1), p.e245, doi:[10.1002/sta4.245](https://doi.org/10.1002/sta4.245).

Examples

See the examples for "mface.sparse".

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